

Please show with steps how you arrive at the final answer

(a) Let $z = 3x^2 - 2xy + x^2y = 2$.

- (i) find the vector which is normal to the curve at (1,1) (3 marks)
- (ii) write down a unit vector \underline{d} along the line $y=x$ and directed at the positive x direction. (2 marks)
- (iii) Find the rate of change of z in the direction of \underline{d} . (2 marks)

(b) The electric intensity of a electrostatic function $V(x,y,z)$ is $E = -\nabla V$

The electrostatic potential produced by a unit dipole-moment, located at the origin and directed along the y -axis, is given by

$$V(x, y, z) = \frac{y}{(x^2 + y^2 + z^2)^{3/2}} \quad (x,y,z) \neq (0,0,0)$$

- (i) Determine the corresponding field-intensity function E . (6 marks)
 - (ii) In what direction, does the potential decreases most rapidly from the point (4,2,4)? (2 marks)
- (c)
- (i) If $\underline{E} = y^2\underline{i} - 3x^2\underline{j} + yz\underline{k}$, find $\nabla \times \underline{E}$ and $\nabla \cdot \underline{E}$ (3 marks)
 - (ii) Show that $\underline{G} = 2xy^3\underline{i} + (1 + 3x^2y^2)\underline{j}$ is conservative vector field on the entire plane. (3 marks)
 - (iii) Find a potential function Φ so that $\nabla\Phi = \underline{G}$. (3 marks)