

Show that if A and B are commutative rings and if $f : A \rightarrow B$ is a ring homomorphism, then there is a natural B -module isomorphism from

$$(B \otimes_A M) \otimes_B (B \otimes_A N)$$

to

$$B \otimes_A (M \otimes_A N)$$

for A -modules M, N .