(d) This is a bonus question, and is not compulsory. Can you show that $J_0(x)$ is a solution of the differential equation

$$xy''(x) + y'(x) + xy(x) = 0?$$

Try substituting the series into the equation.