

The probability density function of X is

$$f(x) = ae^{-ax}, \quad (x > 0).$$

Use this to prove that the corresponding cumulative distribution function (sometimes this is called just the distribution function) is

$$F(x) = 1 - e^{-ax}.$$

Hence find the probability that X is greater than 5 if $a = 0.5$.