Prove that the characteristic functions of subsets satisfy the following

properties :

