Prove that the characteristic functions of subsets satisfy the following

 properties :

 