

10. Griffiths, p. 144, Prob. 3.18. Recall That, In Spherical Coordinates, (r, θ, ϕ) ,

With Imposed Azimuthal Symmetry, $\partial V / \partial \phi = 0$, the Laplace Equation For the

Electrostatic Potential, $\frac{\partial}{\partial r} \left(r^2 \frac{\partial V}{\partial r} \right) + \frac{1}{\sin \theta} \frac{\partial}{\partial \theta} \left(\sin \theta \frac{\partial V}{\partial \theta} \right) = 0$, Can Be Solved

Using a Separation Of Variables, $V(r, \theta) = R(r)\Theta(\theta)$, Where the General

Solution Can Be Written As An Infinite Sum Of Radial Power Law Functions In

Combination With Polar Angle Legendre Polynomials, Which Is

$V(r, \theta) = \sum_{l=0}^{\infty} (A_l r^l + B_l r^{-(l+1)}) P_l(\cos \theta)$, And Where the Coefficients, A_l, B_l , Can Be

Projected Out, Using the Orthonormality Relation For the Legendre Polynomials,

Where $\frac{2l+1}{2} \int_0^{\pi} P_l(\cos \theta) P_{l'}(\cos \theta) \sin \theta d\theta = \delta_{l,l'}$. First, Due To the Infinite Radius

Boundary Condition, $r \rightarrow \infty$, Where $V \rightarrow 0$, You Should Simplify the General

Infinite Sum Solution For the Electrostatic Potential, $V(r, \theta)$, Outside Of the

Sphere, For $r > R$. Next, It Will Be Very Important To Show That the Surface

Potential, $V(R, \theta) = V_0 = k \cos 3\theta$, Can Be Expressed As $V_0 = k(4 \cos^3 \theta - 3 \cos \theta)$,

Where You Could Use the Complex Exponential Representation Of the Cosine

Functions, $\cos(n\theta) = (e^{in\theta} + e^{-in\theta})/2$, And Show That Each Representation Of the