

**Problem 1.4** Use the cross product to find the components of the unit vector  $\hat{n}$  perpendicular to the plane shown in Fig. 1.11.

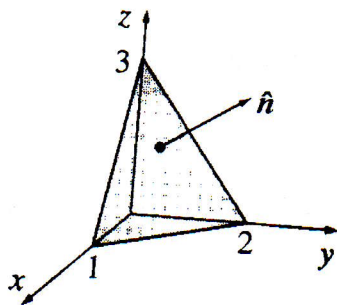


Figure 1.11

**Problem 1.11** Find the gradients of the following functions:

(a)  $f(x, y, z) = x^2 + y^3 + z^4$ .

(b)  $f(x, y, z) = x^2 y^3 z^4$ .

(c)  $f(x, y, z) = e^x \sin(y) \ln(z)$ .

**Problem 1.15** Calculate the divergence of the following vector functions:

(a)  $\mathbf{v}_a = x^2 \hat{x} + 3xz^2 \hat{y} - 2xz \hat{z}$ .

(b)  $\mathbf{v}_b = xy \hat{x} + 2yz \hat{y} + 3zx \hat{z}$ .

(c)  $\mathbf{v}_c = y^2 \hat{x} + (2xy + z^2) \hat{y} + 2yz \hat{z}$ .

**Problem 1.18** Calculate the curls of the vector functions in Prob. 1.15.

**Problem 1.24**

(a) Check product rule (iv) (by calculating each term separately) for the functions

$$\mathbf{A} = x \hat{x} + 2y \hat{y} + 3z \hat{z}; \quad \mathbf{B} = 3y \hat{x} - 2x \hat{y}.$$

A) Use the identity  $\nabla \cdot (\mathbf{A} \times \mathbf{B}) = \mathbf{B} \cdot (\nabla \times \mathbf{A}) - \mathbf{A} \cdot (\nabla \times \mathbf{B})$ , calculate each term and show that the relation is satisfied.