

Notes

15.4

4/24/06

Rectilinear Motion

position/displacement $x(t), s(t)$

velocity $v(t) = s'(t) = \frac{ds}{dt}$

acceleration $a(t) = v'(t) = \frac{dv}{dt} = s''(t) = \frac{d^2s}{dt^2}$

Signs

+

-

$s(t)$: particle is right of the origin

particle is to left of origin

If $s=0$
particle is at origin

$v(t)$: particle moving to the right
(or positive dirn)

particle moving to the left

If $v=0$
particle is stopped

$a(t)$: $v+$ \Rightarrow speeding up

$v+$ \Rightarrow slowing down

$v-$ \Rightarrow slowing down

$v-$ \Rightarrow speeding up

speed = $|v(t)|$

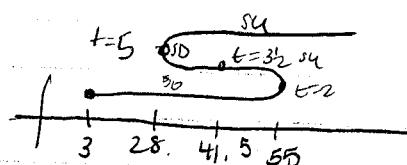
$$s(t) = 2t^3 - 21t^2 + 60t + 3$$

$$v(t) = 6t^2 - 42t + 60 = 0$$

$$t^2 - 7t + 10 = 0$$

$$\checkmark (t-5)(t-2) = 0$$

stopped $t=2, 5$



$$a(t) = 12t - 42 = 0$$

$$t = 3\frac{1}{2} \text{ sec}$$

t	s	v	a	
0	3	+	-	
0-2		+	-	slowing down
2	55	0	-	
$2-3\frac{1}{2}$	"	-	-	speeding up
$3\frac{1}{2}$	41.5	-	0	
$3\frac{1}{2}-5$		-	+	slowing down
5	28	0	+	
>5		+	+	speeding up