

Please show with steps showing how to arrive at the final answer

- (a) Find the work done by the force $\underline{F} = (y - 2x)\underline{i} + (-x)\underline{j}$, as it moves a particle from the point (0,1) to (1,0) along parabola C_1 given by $y = 1 - x^2$, and then return through the 3-quarter unit circle, C_2 centre at the origin, from (1,0) to (0,1)

The 3-quarter circle C_2 can be parametrized by the equations $x = \cos t$,
 $y = -\sin t$ where t goes from $t=0$ to $t = \frac{3\pi}{2}$.

Does the answer remains if C_2 is replaced by another part of the circle, C_3 in opposite direction parametrized by $x = \cos t$, $y = \sin t$ where t goes from $t=0$ to $t = \frac{\pi}{2}$?

(14 marks)

- (b) The region R in the xy -plane is bounded by the lines $x + y = 1$, $y - x = 1$ and $y = 3$.

(i) Sketch the region R ; (2 marks)

(ii) Find the limits of the integration for

$$\iint_R (y^2 - 2x) dx dy \quad \text{and} \quad \iint_R (y^2 - 2x) dy dx; \quad (12 \text{ marks})$$

(iii) Evaluate the integral over R . (3 marks)