Show that $S_5 = Aut(A_5)$.

Please explain your reasoning and solution in as much detail as possible. Thank You.