Show that $S_{5}=\operatorname{Aut}\left(A_{5}\right)$.
Please explain your reasoning and solution in as much detail as possible. Thank You.

