

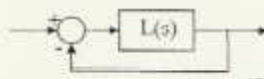
b) Design a proportional and integral controller,  $G = k_p \frac{s + 1/T_i}{s}$  for the plant,  $P = \frac{1}{(s+1)(s+3)}$  to have dominant poles with  $\omega_0 = 1.5$ ,  $\zeta = 0.6$ .

i) Use rough sketches of the root locus to determine the location of the controller zero (i.e. find  $T_i$ ). (Hint: The controller zero is between the plant poles.) (7)

ii) Calculate the required controller gain,  $k_p$ . (An accurate root locus is not required.) (4)

**Question 1: Nyquist analysis**

Consider the following open loop system:  $L = \frac{s+3}{s^2+2}$



- a) Make a rough sketch of the Bode plot (5)
- b) Sketch full Nyquist diagram. (10)
- c) Determine if the closed loop system is stable or not (5)
- d) sketch of the positive gain root locus of the system with open loop transfer function,  $kL(s)$  and comment on your answer in (2c) corresponding to  $k = 1$ . (5)

**Question 3: Root Locus (10 marks)**

Plot the root locus for the following system:  $L = k \frac{s^2 + 2s + 2}{s(s+1)(s+2)}$  as the feedback gain is varied from  $-\infty$  to  $\infty$ .  $1/L(s)$  has turning points at  $s = -1.49$  and  $s = -0.51$ .