

A point x of a measurable set $A \subset \mathbb{R}$ is called a density point if

$$\lim_{h \rightarrow 0} \frac{\ell(A \cap [x - h, x + h])}{2h} = 1$$

where $\ell(B)$ denotes the Lebesgue measure of B . Prove that if A is a set of positive, finite Lebesgue measure, then almost every point of A is its density point.