

Problem 6 (Bonus). Suppose that n is an integer > 1 and a, b are positive integers. Prove that

$$(n^a - 1, n^b - 1) = n^{(a,b)} - 1.$$

(Please show each step of your solution. Thank you.)