

12. Let  $F : \mathbb{R} \times \mathbb{R} \rightarrow \mathbb{R}$  be defined by the equation

$$F(x \times y) = \begin{cases} xy/(x^2 + y^2) & \text{if } x \times y \neq 0 \times 0. \\ 0 & \text{if } x \times y = 0 \times 0. \end{cases}$$

- (a) Show that  $F$  is continuous in each variable separately.
- (b) Compute the function  $g : \mathbb{R} \rightarrow \mathbb{R}$  defined by  $g(x) = F(x \times x)$ .
- (c) Show that  $F$  is not continuous.

(from Continuous Functions)