

For cyclic \mathbb{Z} -modules Z_m and Z_n with generators a and b , respectively, show that $Z_m \otimes_{\mathbb{Z}} Z_n$ is isomorphic to $Z_{(m,n)}$ with generator $a \otimes b$, where (m,n) is the greatest common divisor of m and n .