Prove or disprove each of the following:

 a. The sum of a rational number and an irrational number is an irrational number.

 b. The product of two rational numbers is a rational number.

 c. The product of two irrational numbers is an irrational number.

 d. The product of a rational number and an irrational number is an irrational number.