Prove or disprove each of the following:

a. The sum of a rational number and an irrational number is an irrational number.

b. The product of two rational numbers is a rational number.

c. The product of two irrational numbers is an irrational number.

d. The product of a rational number and an irrational number is an irrational number.