1. a) Let $A$ be a set equipped with a (closed) binary operation $\*$ .

 If $x is$ an arbitrary element of $A$, is $x\*x\*x$ always an associative product?

 Explain. Justify your answer.

 b) Prove or disprove part a. Be complete and thorough in proof writing.