

8. Determine if the following subsets of  $\mathbb{R}$  have upper or lower bounds. Determine the greatest lower bound or the least upper bound.

(a)  $A = \{1, \frac{1}{2}, \frac{1}{3}, \dots, \frac{1}{n}, \dots\}$

(b)  $B = \{1, \frac{1}{2}, \frac{1}{4}, \dots, \frac{1}{2^n}, \dots\}$

(c)  $C = \{1, 1 + \frac{1}{2}, 1 + \frac{1}{2} + \frac{1}{4}, \dots, 1 + \frac{1}{2} + \frac{1}{4} + \dots + \frac{1}{2^n}, \dots\}$

(d)  $D = \{(-1)^n \frac{n+1}{n} : n = 0, 1, 2, 3, \dots\}$

(e)  $E = \{1 + \frac{n+1}{2^n} : n = 0, 1, 2, 3, \dots\}$