4. Let S be the set of all strings of a's and b's. Let R be the relation on S defined by  $\forall x, y \in S, xRy \iff x$  and y begin with different symbols.

Determine, and prove your answers, whether or not  ${\cal R}$  is reflexive, symmetric or transitive.