

I need to plug the solution

$$x(t) = A e^{-\frac{\gamma}{2}t} \cos(\omega_1 t + \phi)$$

into the differential equation

$$\frac{d^2x}{dt^2} + \gamma \frac{dx}{dt} + \omega_1^2 x = 0$$

to get an identity

$$\text{NOTE: } \omega_1 = \sqrt{\omega_0^2 - \frac{\gamma^2}{4}}$$