

Subject to the conditions $x(0) = 0$ and $y(0) = 1$, completely solve the following system of differential equations:

$$\begin{aligned}x' &= x \\ y' &= xy + e^t.\end{aligned}$$
