> Videos

- · What's on the final exam? If your instructor thinks a problem is important enough for a test or quiz, it is probably important enough for the final exam. You should be thinking of the final exam all semester.
- Write all of the test and quiz questions on note cards, one to a card. To prepare for the final, shuffle the cards and try to answer the questions in a random order.

Reading and Writing After reading this section, write out the answers to these questions. Use complete sentences.

- 1. What is the usual first step when solving an equation involving fractions?
- 2. What is a good first step for solving an equation involving decimals?
- 3. What is an identity?
- 4. What is a conditional equation?
- 5. What is an inconsistent equation?
- 6. What is the solution set to an inconsistent equation?

(1) Equations Involving Fractions

Solve each equation by first eliminating the fractions. See Example 1.

7.
$$\frac{x}{4} - \frac{3}{10} = 0$$

8.
$$\frac{x}{15} + \frac{1}{6} = 0$$

9.
$$3x - \frac{1}{6} = \frac{1}{2}$$
 10. $5x + \frac{1}{2} = \frac{3}{4}$

10.
$$5x + \frac{1}{2} = \frac{3}{4}$$

11.
$$\frac{x}{2} + 3 = x - \frac{1}{2}$$

11.
$$\frac{x}{2} + 3 = x - \frac{1}{2}$$
 12. $13 - \frac{x}{2} = x - \frac{1}{2}$

13.
$$\frac{x}{2} + \frac{x}{3} = 20$$

13.
$$\frac{x}{2} + \frac{x}{3} = 20$$
 14. $\frac{x}{2} - \frac{x}{3} = 5$

15.
$$\frac{w}{2} + \frac{w}{4} = 12$$

15.
$$\frac{w}{2} + \frac{w}{4} = 12$$
 16. $\frac{a}{4} - \frac{a}{2} = -5$

17.
$$\frac{3z}{2} - \frac{2z}{3} = -10$$
 18. $\frac{3m}{4} + \frac{m}{2} = -5$

18.
$$\frac{3m}{4} + \frac{m}{2} = -$$

19.
$$\frac{1}{3}p - 5 = \frac{1}{4}p$$
 20. $\frac{1}{2}q - 6 = \frac{1}{5}q$

20.
$$\frac{1}{2}q - 6 = \frac{1}{5}q$$

21. $\frac{1}{6}v + 1 = \frac{1}{4}v - 1$

22.
$$\frac{1}{15}k + 5 = \frac{1}{6}k - 10$$

23.
$$\frac{1}{2}x + \frac{1}{3} = \frac{1}{4}x$$

24.
$$\frac{1}{3}x - \frac{2}{5}x = \frac{5}{6}$$

(2) Equations Involving Decimals

Solve each equation by first eliminating the decimal numbers. See Examples 2 and 3.

25.
$$x - 0.2x = 72$$

26.
$$x - 0.1x = 63$$

27.
$$0.3x + 1.2 = 0.5x$$

28.
$$0.4x - 1.6 = 0.6x$$

29.
$$0.02x - 1.56 = 0.8x$$

$$\mathbf{30.} \ 0.6x + 10.4 = 0.08x$$

31.
$$0.1a - 0.3 = 0.2a - 8.3$$

32.
$$0.5b + 3.4 = 0.2b + 12.4$$

33.
$$0.05r + 0.4r = 27$$

34.
$$0.08t + 28.3 = 0.5t - 9.5$$

35.
$$0.05y + 0.03(y + 50) = 17.5$$

36.
$$0.07y + 0.08(y - 100) = 44.5$$

37.
$$0.1x + 0.05(x - 300) = 105$$

38.
$$0.2x - 0.05(x - 100) = 35$$

(3) Simplifying the Process

Solve each equation. If you feel proficient enough, try simplifying the process, as described in Example 4.

39.
$$2x - 9 = 0$$

40.
$$3x + 7 = 0$$

41.
$$-2x + 6 = 0$$

42.
$$-3x - 12 = 0$$

43.
$$\frac{3}{5} + 1 = 6$$

44.
$$\frac{s}{2} + 2 = 5$$

45.
$$\frac{1}{2} - 3 = -$$

43.
$$\frac{z}{5} + 1 = 6$$
 44. $\frac{s}{2} + 2 = 5$ **45.** $\frac{c}{2} - 3 = -4$ **46.** $\frac{b}{3} - 4 = -7$

47.
$$3 = t + 6$$

48.
$$-5 = y - 9$$

49.
$$5 + 2q = 3q$$

50.
$$-4 - 5p = -4p$$

51.
$$8x - 1 = 9 + 9x$$

52.
$$4x - 2 = -8 + 5x$$

53.
$$-3x + 1 = -1 - 2x$$

54.
$$-6x + 3 = -7 - 5x$$

(4) Identities, Conditional Equations, and Inconsistent Equations

Solve each equation. Identify each as a conditional equation, an inconsistent equation, or an identity.

See Examples 5 and 6.

See Recognizing Identities and Inconsistent Equations on page 107.

55.
$$x + x = 2x$$

56.
$$2x - x = x$$

57.
$$a-1=a+1$$

58.
$$r + 7 = r$$

59.
$$3y + 4y = 12y$$

60.
$$9t - 8t = 7$$

61.
$$-4 + 3(w - 1) = w + 2(w - 2) - 1$$

62.
$$4 - 5(w + 2) = 2(w - 1) - 7w - 4$$

63.
$$3(m+1) = 3(m+3)$$

64.
$$5(m-1) - 6(m+3) = 4 - m$$

65.
$$x + x = 2$$

66.
$$3x - 5 = 0$$

67.
$$2 - 3(5 - x) = 3x$$

68.
$$3 - 3(5 - x) = 0$$

69.
$$(3-3)(5-z)=0$$

70.
$$(2 \cdot 4 - 8)p = 0$$

71.
$$\frac{0}{x} = 0$$

72.
$$\frac{2x}{2} = x$$

73.
$$x \cdot x = x^2$$

74.
$$\frac{2x}{2x} = 1$$

Miscellaneous

Solve each equation.

75.
$$3x - 5 = 2x - 9$$

76.
$$5x - 9 = x - 4$$

77.
$$x + 2(x + 4) = 3(x + 3) - 1$$

78.
$$u + 3(u - 4) = 4(u - 5)$$

79.
$$23 - 5(3 - n) = -4(n - 2) + 9n$$

80.
$$-3 - 4(t - 5) = -2(t + 3) + 11$$

81.
$$0.05x + 30 = 0.4x - 5$$

82.
$$x - 0.08x = 460$$

83.
$$-\frac{2}{3}a + 1 = 2$$

84.
$$-\frac{3}{4}t = \frac{1}{2}$$

85.
$$\frac{y}{2} + \frac{y}{6} = 20$$

86.
$$\frac{3w}{5} - 1 = \frac{w}{2} + 1$$

87.
$$0.09x - 0.2(x + 4) = -1.46$$

88.
$$0.08x + 0.5(x + 100) = 73.2$$

89.
$$436x - 789 = -571$$

90.
$$0.08x + 4533 = 10x + 69$$

91.
$$\frac{x}{344} + 235 = 292$$

92.
$$34(x-98) = \frac{x}{2} + 475$$

(5) Applications

Solve each problem. See Example 7.

93. *Sales commission.* Danielle sold her house through an agent who charged 8% of the selling price. After the commission was paid, Danielle received \$117,760. If *x* is the selling price, then *x* satisfies

$$x - 0.08x = 117,760.$$

Solve this equation to find the selling price.

94. *Raising rabbits.* Before Roland sold two female rabbits, half of his rabbits were female. After the sale, only one-third of his rabbits were female. If *x* represents his original number of rabbits, then

$$\frac{1}{2}x - 2 = \frac{1}{3}(x - 2).$$

Solve this equation to find the number of rabbits that he had before the sale.

- **95.** *Eavesdropping.* Reginald overheard his boss complaining that his federal income tax for 2006 was \$60,531.
 - a) Use the accompanying graph to estimate his boss's taxable income for 2006.
 - b) Find his boss's exact taxable income for 2006 by solving the equation

$$42,170 + 0.33(x - 188,450) = 60,531.$$