

Let  $g(x) = x^2 + x - 1$  and let  $h(x) = x^3 - x + 1$ . Obtain fields of 4, 8, 9 and 27 elements by adjoining a root of  $f(x)$  to the field  $F$  where  $f(x) = g(x)$  or  $h(x)$  and  $F = \mathbb{F}_2$  or  $\mathbb{F}_3$ . Write down the multiplication tables for the fields with 4 and 9 elements and show that the nonzero elements form a cyclic group.