

p1alg

What are the partial fraction decompositions (sum of terms of the forms  $\frac{A}{(z - a_i)^{k_i}}$ ) for

a)  $f(z) = \frac{1}{z^4 - z^2}$

b)  $f(z) = \frac{1}{z^2 + 1}$

c) What are the values of  $\int_{\Gamma^4} f(z) dz$  for the above choices of  $f(z)$ ?

2. Find  $\int_{\Gamma^{2_0}} \frac{z dz}{z^2 + 1}$  by

a) residual calculation

b) by writing  $\frac{z}{z^2 + 1} = \frac{1}{2} \frac{d}{dz} \log(z^2 + 1)$ . Why are the results the same?

c) Same question for  $\int_{\Gamma^{1/2}} \frac{z dz}{z^2 + 1}$