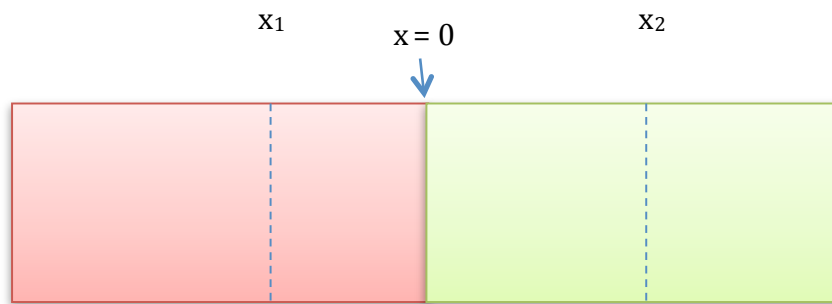


**Problem 2:**

A p-n junction is formed by bringing two pieces of crystalline silicon (c-Si) into contact as shown below. Phosphorous atoms, at a concentration of  $5.0 \times 10^{15} \text{ cm}^{-3}$ , are dopants on the left side, while boron atoms are dopants on the right at a concentration of  $3.0 \times 10^{16} \text{ cm}^{-3}$ . For both the phosphorus-doped and boron-doped sides, the dopant atoms are distributed uniformly. Note that the drawing may not be to scale. The device is in the dark, and all of the dopants are ionized. The region  $x_1 < x < x_2$  is the depletion region.

- a. Define (and describe in words) variables  $N_A$  and  $N_D$



- b. Label the drawing above to clearly indicate which side is the p-type silicon, and which is the n-type silicon.
- c. What is the source of the charge density and the value of the charge density (in Coulombs per  $\text{cm}^3$ , to two significant figures) at  $x = x_1/2$ ?
- d. If we take the intrinsic carrier concentration to be  $1.0 \times 10^{10} \text{ cm}^{-3}$ , what is the value of the built-in potential ( $V_{bi}$ ) to two significant figures? Calculate and graph  $V_{bi}$  as a function of temperature over the range of temperatures experienced by North America:  
[http://en.wikipedia.org/wiki/Extremes\\_on\\_Earth](http://en.wikipedia.org/wiki/Extremes_on_Earth) As always, clearly label your axes, and include units.
- e. Use the dielectric constant of silicon to calculate the electric field gradient,  $\partial E / \partial x$ , at  $x = x_1/2$ ? Express your answer in units of  $\text{V/cm}^2$ . Explain how the dielectric constant of Si is related to the permittivity of free space.
- f. Calculate the values of  $x_1$  and  $x_2$  in cm. What fraction of the device thickness is in the depletion region if the total thickness of the solar cell is  $200 \mu\text{m}$  thick?
- g. Check whether or not we have charge neutrality (i.e., zero net charge) over the region from  $x_1$  to  $x_2$ . Recall that we have no free carriers (electrons or holes) in this region.

h. Write the equations needed to solve for the electric field strength over the region  $x_1$  to  $x_2$ . Specify the boundary conditions and use these to solve the equations. Compute and graph the electric field as a function of position from  $x_1$  to  $x_2$ . Label your axes, including appropriate units for the x- and y-axes. What is the value of the electric field for  $x < x_1$ , outside the depletion region?

i. Solve for the potential as a function of position, and graph the results from  $x_1$  to  $x_2$  (define the potential to be equal to zero at  $x = x_2$ ). Label the axes appropriately, and add any additional detail required to demonstrate understanding. Look at the value of the potential change from one side of the depletion region to the other. Is this physically realistic (briefly explain your answer)?

j. With this potential profile, a photon is absorbed within the depleted region. Which way do the electron and hole move under the influence of the electric field? Use an 'e-' and an 'h+' along with arrows to show their drift directions.