2. Show that for a system described by the Hamiltonian $\hat{H}$,

$$E_0 \leq \langle \psi | \hat{H} | \psi \rangle \,,$$

where E_0 is the lowest energy of the system, and $| \psi \rangle$ is any normalized state. Explain why this fact is useful.