5. Suppose that $\{p_n\}$ is a sequence which converges to some number p. Prove that there is at most one number α for which

$$\lim_{n \to \infty} \frac{|p_{n+1} - p|}{|p_n - p|^{\alpha}}$$

is a positive, finite number.