

9. Let  $a$  be a fixed number with  $a > 0$ . Set

$$g(x) = \frac{x^3 + 3ax}{3x^2 + a}.$$

Define a sequence  $\{p_n\}$  by  $p_{n+1} = g(p_n)$  and suppose that  $p_0$  has been chosen so that the sequence  $\{p_n\}$  converges to a number  $p > 0$ . What is  $p$ ? Show that the order of convergence is equal to 3.