

- (f) Calculate the energy released when a thermal neutron is captured by the nucleus of a  $^{235}\text{U}$  atom that then fissions to produce  $^{137}\text{Cs}$ ,  $^{97}\text{Zr}$  and two neutrons.  
 [Atomic masses:  $n=1.0087\text{u}$ ,  $^{235}\text{U}=235.0439\text{u}$ ,  $^{137}\text{Cs}=136.9070\text{u}$ ,  $^{97}\text{Zr}=96.9110\text{u}$ ,  
 $1\text{u}=931.48\text{ MeV}/c^2$ ]

- (g) Show that the reactor equation  $\nabla^2\Phi + 3(\bar{k}_\infty - 1)\bar{\Sigma}_A\bar{\Sigma}_S\Phi = 0$  has solutions of the form

$$\Phi = A \cos(k_1x) \cos(k_2y) \cos(k_3z),$$

where  $x, y, z$  are the variables and  $k_1, k_2, k_3$  are constants.

If the reactor takes the form of a cube of side  $a$ , with the origin for the  $xyz$  coordinate system at the cube centre, show that  $k_1 = k_2 = k_3 = \pi/a$  and that

$$(\bar{k}_\infty - 1)\bar{\Sigma}_A\bar{\Sigma}_S = \frac{\pi^2}{a^2}.$$