

1. Find a **parametric** representation of the curve:

$$x^2 + y^2 = 36 \text{ and } z = \frac{1}{\pi} \arctan\left(\frac{x}{y}\right).$$

i.e. find a representation in the form: $x = x(t); y = y(t), z = z(t)$.

2. Find what kind of curves are given by the following representations and **draw (schematically)** the curves:

(i) $\underline{r(t)} = (2t - 5, -3t + 1, 4)$;

(ii) $\underline{r(t)} = (0, -\cos(t), 3\sin(t))$

3. Find the equations of the tangent (straight line) and the normal plane to the curve given by the following **parametric** representation:

$$x = 2 + 3t^4; y = 2t + t^3, z = t \text{ at the point } t = 1.$$

4. The equations of motion of a point particle in space are given by:

(i) $\underline{x(t)} = 2t^3 - 3$; $\underline{y(t)} = -3t^3$; $\underline{z(t)} = 4t^3 - 1$.

(ii) $\underline{x(t)} = a \sin(\omega t)$; $\underline{y(t)} = a \cos(\omega t)$; $\underline{z(t)} = t$

In each case, calculate the **velocity vector** \underline{v} and the **acceleration vector** \underline{a} . Also calculate the absolute values of these vectors. What are the curves along which the particle moves?

(find these values for an arbitrary t , with a and ω being fixed parameters)