

Solve the equation  $z^2 + z + 1 = 0$  using  $z = (x, y)$  and the basic definitions.  
(Hint: Note that  $y \neq 0$  because the equation  $x^2 + x + 1 \neq 0$  for any real number  $x$ .)

a.

$$z_1 = -1 + j\frac{\sqrt{3}}{2} \text{ and } z_2 = -\frac{1}{2} - j\frac{\sqrt{3}}{2}$$

b.

$$z_1 = -\frac{1}{2} + j\frac{\sqrt{3}}{2} \text{ and } z_2 = -\frac{1}{2} - j\frac{\sqrt{3}}{2}$$

c.

$$z_1 = -\frac{1}{3} + j\frac{\sqrt{3}}{2} \text{ and } z_2 = -j\frac{\sqrt{3}}{2}$$

d.

$$z_1 = \frac{3}{2} + j\frac{\sqrt{3}}{2} \text{ and } z_2 = -\frac{1}{2} - j\frac{\sqrt{3}}{4}$$