

2. If we assume a solution for the Sine Gordan equation of the form $\sigma(u, v) = 4 \tan^{-1} \left[\frac{U(u)}{V(v)} \right]$.

What are the equations satisfied by U and V ? Show that $\sigma = 4 \tan^{-1} \left(\gamma e^{\left(ax + \frac{t}{a} \right)} \right)$ is a solution.

Find some other solutions of this form

$$u = ax + t/a$$

$$v = ax - t/a$$

$$\sigma_{UU} - \sigma_{VV} = \sin \sigma$$

$$\sigma_{UV} = \sin \sigma$$