

Show that two integrals of E,

$$E = \frac{1}{4\pi\epsilon_0} \int_{v'} \frac{\rho}{r^2} \hat{r} dv' \quad \text{and} \quad E = - \frac{1}{4\pi\epsilon_0} \int_{v'} \nabla' \cdot \frac{\rho}{r} dv'$$

Are equal, at least if v' is infinite.

Now, show that as a consequence of

$$E = \frac{1}{4\pi\epsilon_0} \int_{v'} \frac{\rho}{r^2} \hat{r} dv' \quad \text{and} \quad E = - \frac{1}{4\pi\epsilon_0} \int_{v'} \nabla' \cdot \frac{\rho}{r} dv',$$

$$\text{that} \quad \int_{v'} \nabla' \cdot \frac{\rho}{r} dv' = 0$$