

## Problem

Let  $A$  be a square  $n \times n$  matrix over  $C[X]$  and write  $A = [p_{jk}(X)]$ .

For any  $z \in C$  ( $z$  being a complex variable) let  $A(z) := [p_{jk}(z)]$ , that is a square  $n \times n$  matrix over  $C$ .

Show that matrix  $A$  is invertible if and only if matrix  $A(z)$  is invertible for all  $z$  from  $C$ .

Will it be still valid if we change complex numbers into set of real ?